Dear [Recipient's Name],

I hope this message finds you well. I am writing to sincerely apologize for not responding to your [email/letter/message] in a more timely manner. I appreciate your patience and understanding regarding my delay.

The past few weeks have been quite hectic for me, and I regret any inconvenience my late response may have caused you. Your communication was important to me, and I truly value our [relationship/correspondence].

Thank you for your understanding, and I look forward to continuing our conversation. Please feel free to reach out if there's anything you would like to discuss further.

Warm regards,

[Your Name]

[Your Position]

[Your Contact Information]