Dear Professor [Last Name],

I hope this message finds you well. I wanted to take a moment to express my sincerest gratitude for the recommendation you provided on my behalf for [specific program, job, etc.].

Your support and belief in my abilities mean so much to me, and I truly appreciate the time you took to craft such a thoughtful letter. Your insights and encouragement have not only strengthened my application but have also motivated me to strive for excellence.

Thank you once again for your help and guidance. I look forward to keeping you updated on my progress.

Warm regards, [Your Name] [Your Contact Information]